

Research Article

## Comparative study of different exponential smoothing models in simulation of meteorological drought : A study on Purulia district, West Bengal, India

### Shrinwantu Raha\*

Department of Geography, Coochbehar Panchanan Barma University, Coochbehar-736101 (West Bengal), India

### Shasanka Kumar Gayen

Department of Geography, Coochbehar Panchanan Barma University, Coochbehar-736101 (West Bengal), India

\*Corresponding author. Email: rahashrinwantu@gmail.com

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### Abstract

Drought is a burning issue in India and hence needs serious attention of researchers to develop rigorous plan and management. Areas that belong to various plateaus, e.g., Chottanagpur plateau, Deccan plateau, etc., are mostly affected by drought in India. In the past decade, Purulia District of West Bengal, which belongs to northeast part of Chottanagpur plateau, faced severe drought several times. But the assessment of drought in this area was far from a decisive proclamation till date. In this research, an attempt was made to compare the Holt-Winter additive and Holt-Winter multiplicative model in simulation (at 1 month lead time) of meteorological drought (using Standardized Precipitation Index (SPI) of Purulia District, West Bengal, India. The additive model showed better performance than the multiplicative model with minimized Root Mean Squared Error (RMSE) and higher correlation coefficient value ( $R^2$ ). The spatial assessment drought at pre-monsoon, monsoon and post-monsoon phase indicated that severe drought had occurred in post monsoon and premonsoon phase at the eastern portions of the study area.

**Keywords:** Additive Model, Multiplicative model, Standardized Precipitation Index (SPI)

### INTRODUCTION

Drought is a slow onset, costliest, recurrent and complex phenomenon (Drumond *et al.*, 2017). It is very difficult to describe its status most of the time because of its' inherent character (Rossi 2003). The general feature of drought is peculiar, which significantly deviates from other natural hazards and disasters (Zarch *et al.*, 2015) as it may stretch over a month or even years (Singh *et al.*, 2019). Over 4 types of drought (e.g. meteorological drought, hydrological drought, ecological drought and socioeconomic drought), meteorological drought is more common and complex in nature (Stagge *et al.*, 2015). Its' complexity further increases when it assimilates with other meteorological and socioeconomic phenomena (Dogan *et al.*, 2012). Drought forecasting and simulation is an essential element in drought risk management (Hagenlocher *et al.*, 2019). Although considerable works have been done in spatio-

temporal assessment of drought, still simulation and prediction of drought are relatively new and challenging aspects in weather forecasting (Yves *et al.*, 2020). This research tried to utilize the exponential smoothing models to simulate the meteorological drought, completely new in this field. Thus this research bears the fo two objectives a) To simulate meteorological drought at 1 month lead time using two exponential smoothing models, b) To make a comparative assessment of two exponential smoothing models to determine which model is a better fit for this context.

### MATERIALS AND METHODS

#### Study area

Purulia is one of the westernmost districts of West Bengal and it is an extended tract of Rarh terrain (Dey *et al.*, 2020). This region is affected by the shortage of rainfall and due to low water holding capacity of the

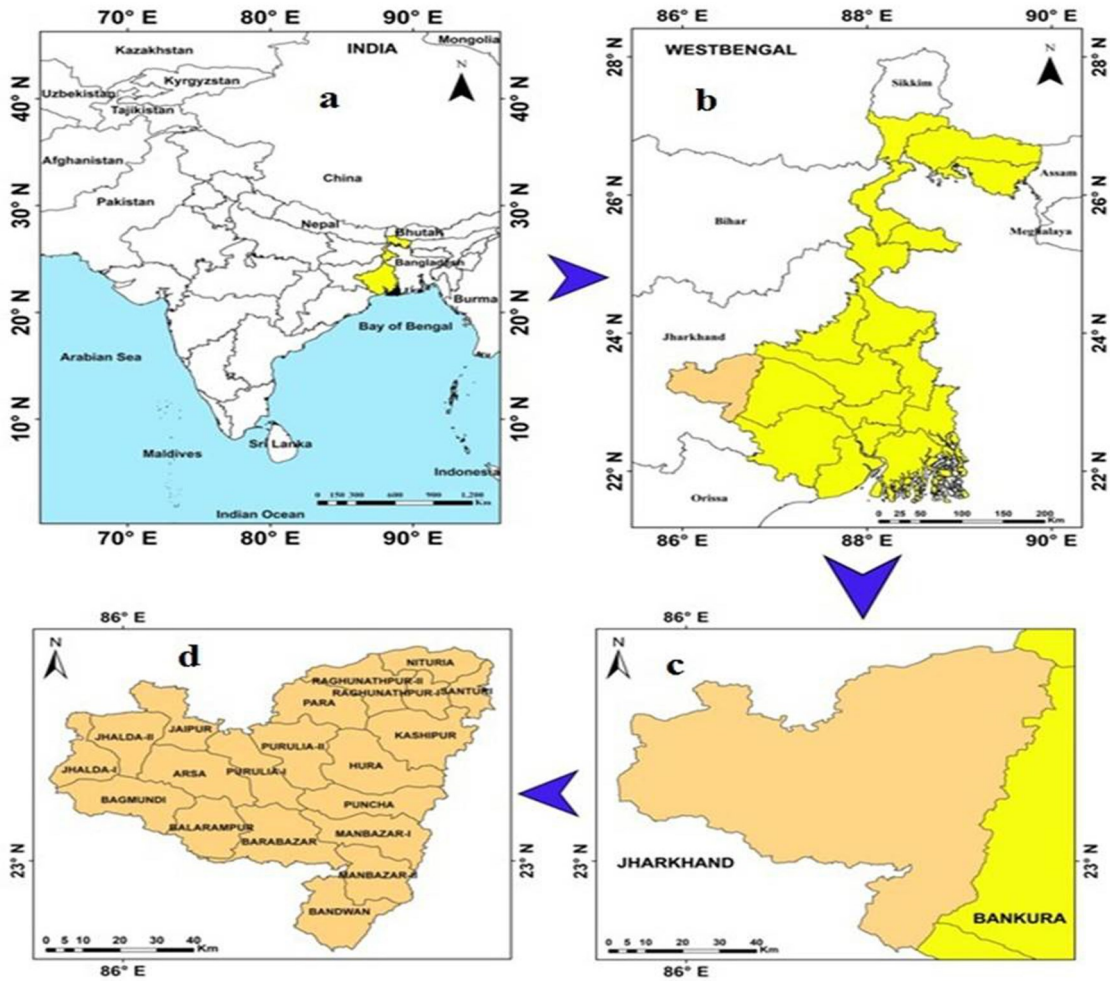


Fig. 1 Location map of Purulia District.

soil, 50% of its' rainfall passes away as runoff (Hazra *et al.*, 2017). Average annual rainfall varies between 1100 to 1500 mm within Purulia. 75% to 90% relative humidity is observed in monsoon season. According to SAFE (2011), Purulia was the worst hit, with agricultural production falling to 27% and around 280,000 hectares of agricultural land was lying vacant facing drought. Most of the families of Purulia (almost 70-75%) were dependent upon paddy production and the drought condition of 2010 had put an end to their only means of livelihood. Therefore effective early warning system of drought is desperately needed to combat the situation in Purulia. Simulation of drought helps to understand the true nature of drought and helps to perceive the severity of drought in the near future. Fig. 1 depicts the location map of the study area.

**Source of data**

Rainfall data was downloaded from Climate Forecast System Reanalysis (CFSR) Soil and Water Assessment daily database and those daily databases were converted into monthly values. CFSR is an open access high resolution coupled atmosphere-ocean-land-surface-sea ice system which provides the best estimate of these

coupled domains over 1979-2013 period completely. Fig. 2 denotes the stations' name, location, mean and standard deviation of rainfall. SPI was simulated by Holt-Winter additive and Holt-Winter multiplicative models and ultimately superiority of every model were judged using statistically robust Root Mean Squared Error (RMSE), and R<sup>2</sup> value. Fig. 3 denotes methodological framework of this research.

**Standardized precipitation index (SPI)**

Mckee *et al.* (1993) proposed that SPI is found suitable to monitor drought events worldwide (Durdu 2010). This research strictly follows the scheme of Mckee *et al.*, (1993) for the calculation of SPI which is as follows: The first step is to determine the cumulative difference between total rainfall data points and long term rainfall means (Sönmez *et al.*, 2005). The rainfall data points at j-th time frame are denoted as  $x_{ij}$ , mean of the rainfall (at j-th time frame) is denoted as  $\bar{x}_j(\alpha)$  and the standard deviation of rainfall (i-th data point and j-th time step) is denoted as  $\delta_{ij}$  so the initial equation is as follows:

$$SPI = \frac{x_{ij} - \bar{x}_j}{\delta_{ij}} \tag{1}$$

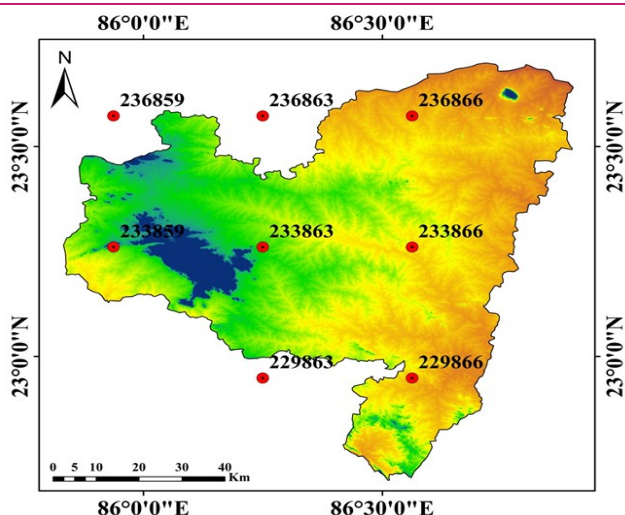


Fig. 2. Location of meteorological station of Purulia District .

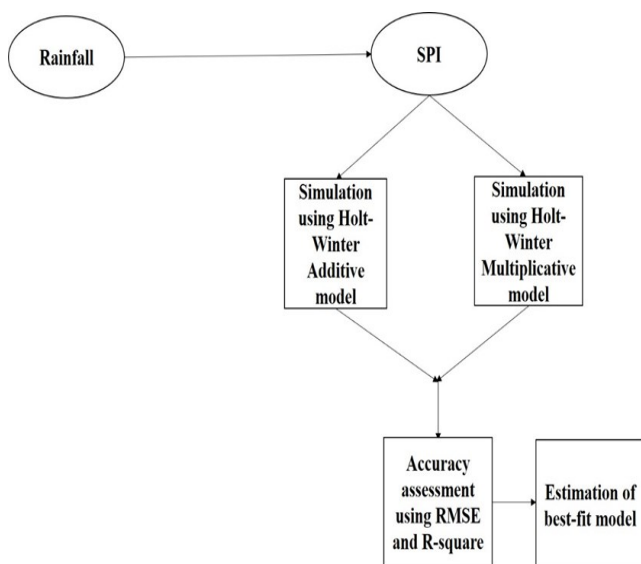


Fig. 3. Methodological framework.

Thom (1958) found that the gamma distribution function can be utilized to fit the various climatological time series in a structured manner. So, in the next step the rainfall series is fitted with gamma probability distribution function (Thom 1958) which is denoted as follows:

$$P(x) = \frac{1}{\beta^{\alpha} \Gamma(\alpha)} x^{\alpha-1} e^{-\frac{x}{\beta}} \tag{2}$$

$$SPI = \frac{x_{ij} - P(x)}{\delta_{ij}} \tag{3}$$

Here, P denotes the gamma probability distribution function.

Here, the appearance of parameters is denoted by  $\alpha$  and the range of the parameter is denoted by  $\beta$ , x denotes the amount of rainfall, and  $\Gamma(\alpha)$  is the gamma function. The value of  $\alpha$  and  $\beta$  is greater than 0.  $\Gamma(\alpha)$  can be written as follows:

$$\Gamma(\alpha) = \lim_{n \rightarrow \infty} \frac{n! n^{\alpha-1}}{y^{\alpha}} \equiv \int_0^{\infty} y^{\alpha-1} e^{-y} dy \tag{4}$$

Here,  $\alpha$  and  $\beta$  are estimated using maximum likelihood solutions (Thom 1958) which is as follows:

$$\tilde{\alpha} = \frac{1}{4A} \left( 1 + \sqrt{1 + \frac{4A}{3}} \right) \tag{5}$$

$$\tilde{\beta} = \frac{\bar{x}}{\tilde{\alpha}} \tag{6}$$

Where,

$$A = \ln(\bar{x}) - \frac{\sum \ln(x)}{n} \tag{7}$$

After that  $\alpha$  and  $\beta$  are adopted to detect the increasing probability distribution function  $p'(x)$  at a selected time step

$$p'(x) = \int_0^x P(x) dx = \frac{1}{\beta^{\alpha} \Gamma(\alpha)} \int_0^x x^{\alpha-1} e^{-x/\beta} dx \tag{8}$$

Rainfall is not always continuous over time. In this research, zero values are considered as the no rainfall. True feasibility of non exceedence was proposed by Edwards and Mckee (1997) which can be obtained as follows:

$$H(x) = q + (1 - q)p'(x) \tag{9}$$

Where, q is obtained using the method of Thom (1958)

$$q = \frac{m}{n} \tag{10}$$

q is the possibility of zero event, m is the frequency of zero event in the rainfall dataset.

### Holt-winter exponential smoothing

Holt-Winter exponential smoothing is a statistical method which is used here to simulate drought at 1 month lead time. It provides an effective way of forecasting of future value of time series data (Razali *et al.*, 2018).  $\alpha$ ,  $\beta$ ,  $\gamma$  are the 3 smoothing constants are required for updating the level, trend and seasonal index respectively at time, t. The value of these constants lies between 0 to 1 (Elmunim *et al.*, 2015). This value is selected depending on the weight (high smooth constant mean ensures more weight). Holt-Winter method has two seasonal models i.e. additive and multiplicative. Here, monthly SPI ( $R_t$ ) is assessed from monthly rainfall dataset. Additive and multiplicative model is applied for SPI separately in this research using following equations (Hyndman and Athanasopoulos, 2018):

Simulation and prediction of SPI using Additive Model:

$$\begin{cases} L_t = \alpha_1(R_t - S_{t-s}) + (1 - \alpha_1)(L_{t-1} + b_{t-1}) \\ b_t = \beta_1(L_t - L_{t-1}) + (1 - \beta_1)b_{t-1} \\ S_t = \lambda_1(R_t - L_t) + (1 - \lambda_1)S_{t-s} \\ F_{t+m} = L_t + b_t m + S_{t-s+m} \end{cases} \tag{11}$$

Where,  $L_t$  is the level,  $b_t$  is the trend,  $S_t$  is the seasonal factor,  $R_t$  is the actual monthly SPI, and  $t$  is the time period of  $L_t$ ,  $b_t$ ,  $S_t$  and  $R_t$  component.  $S$  is the number of seasons of a year, here monthly data has been used so  $S = 12$ .  $S = 11^{th}$  month (i.e. November) to  $2^{nd}$  month (i.e. February) is considered as post monsoon season,  $S = 3^{rd}$  month (i.e. March) to  $5^{th}$  month (i.e. May) considered as pre-monsoon season and rest of the period i.e.  $6^{th}$  month (i.e. June) to  $10^{th}$  month (i.e. October) is considered as the monsoon season.  $F_t$  is the forecast value of  $R_t$  ahead of six period,  $F_{t+m}$  is the monthly forecasted time period;  $\alpha$ ,  $\beta$ ,  $\lambda$  level, trend and seasonal smoothing coefficient estimators respectively,  $m$  is the forecast period and  $S_t$  is the seasonal duration. The initial value of seasonal component  $S_1$  determined using eq. 12 (Granger and Newbold 1986),

$$S_1 = R_1 - L_s, \quad S_2 = R_2 - L_s, \quad \dots \dots \dots$$

$$S_s = R_s - L_s \tag{12}$$

$$L_s = \frac{1}{s} (R_1 + R_2 + R_3 + \dots \dots \dots R_s) \tag{13}$$

Simulation and prediction of SPI using Multiplicative model:

$$\begin{cases} L_t = \alpha_1 \frac{R_t}{S_{t-s}} + (1 - \alpha_1)(L_{t-1} + b_{t-1}) \\ b_t = \beta_1 (L_t - L_{t-1}) + (1 - \beta_1)b_{t-1} \\ S_t = \lambda_1 \frac{Y_t}{L_t} + (1 - \lambda_1)S_{t-s} \\ F_t = (L_{t-1} + b_{t-1})S_{t-s} \\ F_{t+m} = (L_t + b_t m)S_{t-s+m} \end{cases} \tag{14}$$

The initial seasonal component value ( $S_1$ ) and the level of seasonal duration  $s$  is determined by the following equations (15) and (16)

$$S_1 = \frac{R_1}{L_s}, S_2 = \frac{R_2}{L_s}, \dots \dots \dots S_t = \frac{R_t}{L_s} \tag{15}$$

$$L_s = \frac{1}{s} (R_1 + R_2 + \dots \dots \dots + R_s) \tag{16}$$

**Accuracy Assessment**

Error estimation judges the statistical significance of the models. The RMSE and  $R^2$  are utilized here which can be expressed as follows:

**Root Mean Squared Error (RMSE)**

Root Mean squared error (RMSE) is calculated using the following equation (Hyndman and Athanasopoulos 2018):

$$RMSE = \sqrt{\frac{1}{n} (F_t - F'_t)^2} \tag{17}$$

Where,  $n$  is the number of observations,  $F_t$  is the actual

value,  $F'_t$  is the forecasted value at period  $t$ . We use constant multiplicative factors to adjust the variability, randomness and validation of the data set  $z$ . Lower the Mean Square Error higher the accuracy and vice versa (Wichitarapongsakun *et al.*, 2016). For the convenient and sophisticated use this research adjusts RMSE within 0 to 1 for pictorial representation.

**Assessment of correlation coefficient ( $R^2$ ) value:**

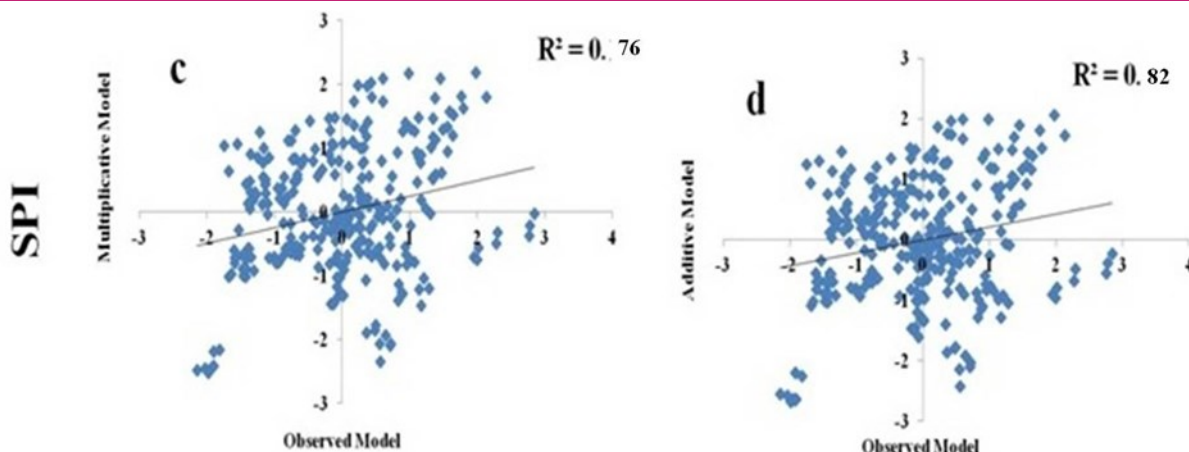
Appraisal of precision of different simulation models can be estimated by correlation-coefficient ( $R^2$ ) value (Suryanarayana and Mistry 2016). Pearson's product moment correlation coefficient is the robust statistical technique which can be utilized to estimate efficiency of statistical models (Kamari *et al.*, 2013).  $r$  is expressed as follows:

$$r = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}} \tag{18}$$

Where,  $r$  is the correlation coefficient;  $x_i$  is the observed value and  $y_i$  is the modelled value at time  $i$ ,  $\bar{x}$  and  $\bar{y}$  is the average value of observed and modelled value,  $n$  is the number of observations.

**RESULTS**

The month to month variation of the actual and forecasted SPI of 8 meteorological stations for the period of 1979-2013 are shown in Fig. 5. The observed and simulated SPI showed inter and intra-seasonal variation of peaks (at rainy season) and drops (at dry season) at all the stations. The seasonally simulated SPI for all the meteorological stations varied between -3 to 2.5. From Fig. 5, it was obvious that in all stations, droughts were occurring in the pre-monsoon and post-monsoon period. Station 233859, 229866 and 233866 exhibited the same nature of seasonal variation (Fig. 5), which was increased slightly with the significant difference between actual and forecasted SPI during post-monsoon phase, especially for the months of November-December. Additive models achieved a higher correlation coefficient ( $R^2$ ) value (i.e. 0.82) in relation to the respective observed model (Fig. 4). Relatively low RMSE (0.235) was produced by Additive model in simulation of drought. The additive model produced better result and this result could be very essential to know the present and future conditions of drought of Purulia. The spatial assessment of pre-monsoon, monsoon, and post monsoonal SPI (Fig. 6) indicates that in most cases, the eastern portions of the district face highest drought (lowest SPI) using all models. Using all models, average pre-monsoonal SPI (Fig. 6a, 6b, 6c) varied within -2.344 to -0.635. In the monsoon season SPI (Fig. 6d, 6e, 6f) varied within -3.218 to -0.603 (using all models) whereas in the post monsoon season average



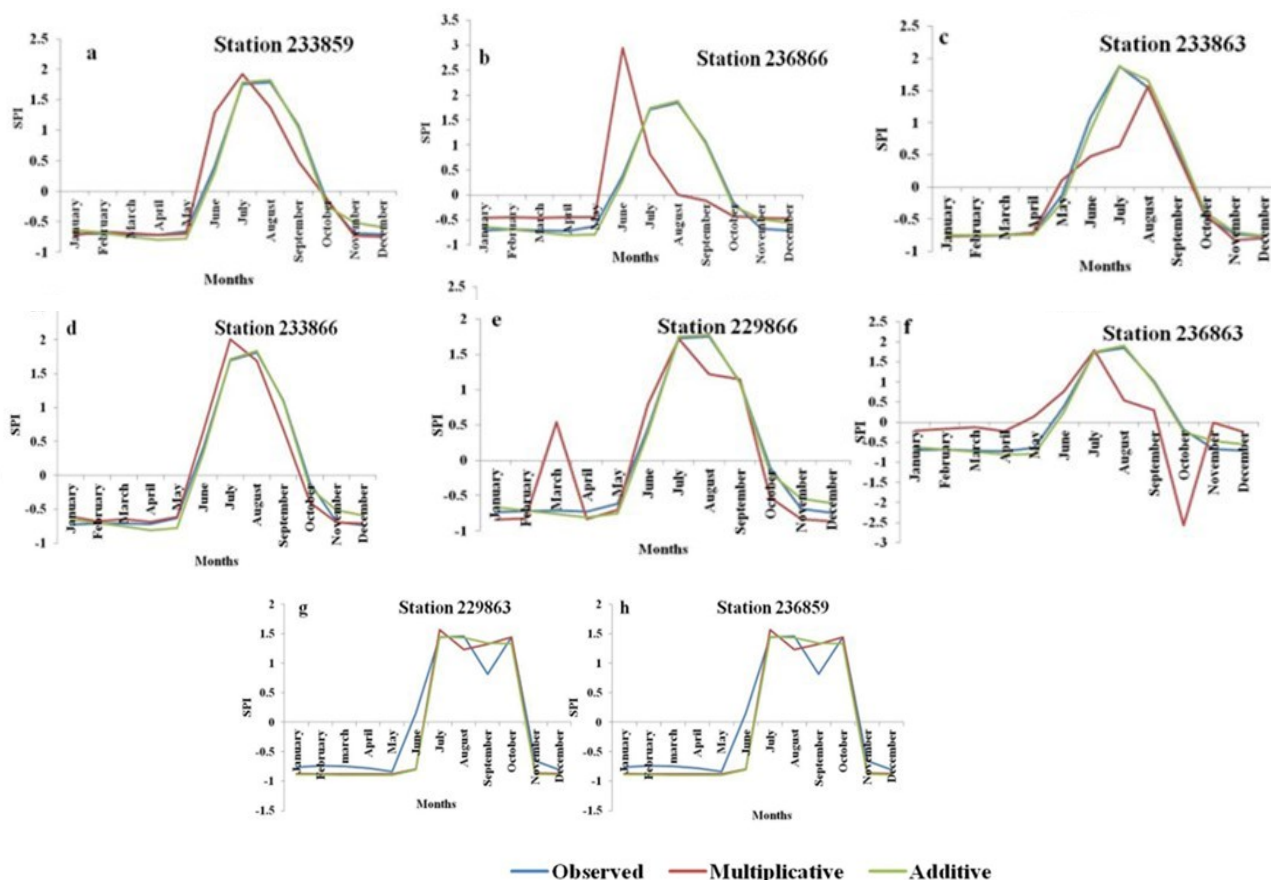
**Fig. 4.** Showing correlation between observed and simulated models (at 1 month lead time) c) Correlation between observed and multiplicative model d) Correlation between observed and additive model.

SPI (Fig. 6g, 6h, 6i) varied within -3.218 to -0.603 (using all models). According to the observed model, drought was high at the western portions at pre monsoon season and it was low at the eastern portions. At post-monsoon season, northern and north-eastern portions were noticed with high drought and southern portions with low drought. At monsoon and post monsoon season similar feature was noticed. In the case of the multiplicative model, the middle and western portions of

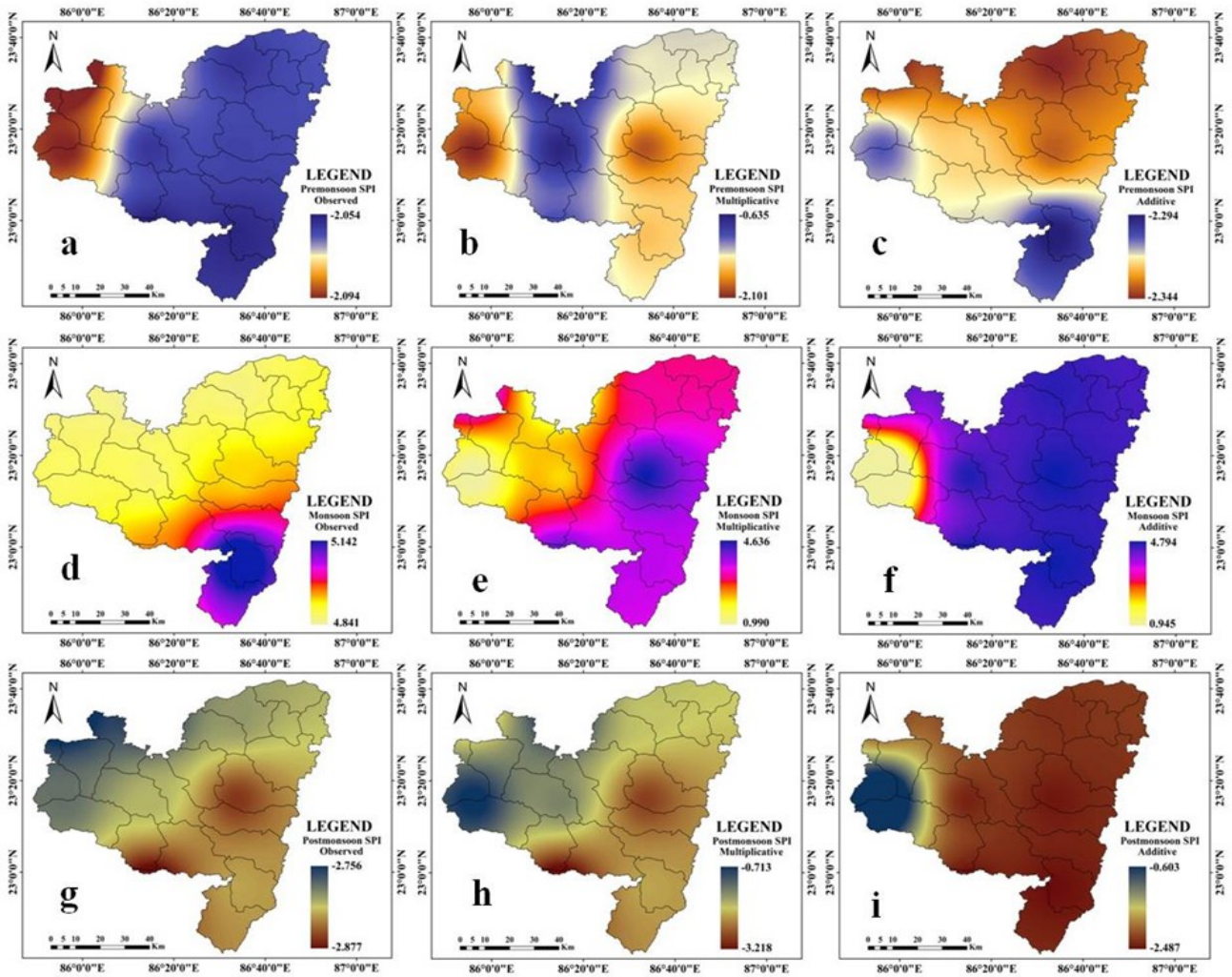
the study region were observed with relatively high drought in pre-monsoon, monsoon and post monsoon seasons.

### DISCUSSION

The drought of Purulia matches with West Bengal as well as all India pattern (Chatterjee *et al.*, 2016). The possible causes of such a picture are deeply rooted in



**Fig. 5.** Showing station wise assessments of observed and simulated SPI (at 1 month lead time).



**Fig. 6.** Showing spatial assessment of SPI using observed and simulated models (at 1 month lead time) in pre-monsoon, monsoon and post-monsoon phase.

geo-environmental condition as well as global climate change. The seasonal pattern of drought with ENSO (i.e. the warm ENSO event is associated with weak Indian Monsoon) experiences maximum positive relationship in the last 40 years (Kripalani *et al.*, 2003). The southeast ward shift of walker circulation anomalies and higher surface temperatures in winter and spring creates an enormous impact on this changing relationship (Kumar, 1999). Hence the ENSO event cannot truly express the variability of drought in the Indian sub-continent as well as for Purulia. Broadly the drought in West Bengal as well as in India depends on a number of factors, i.e., ‘weakening of easterly jet, ‘warming of equatorial Indian Ocean than northern latitudes of the tropics’, ‘weakening of gradient of Sea Surface Temperature (SST) from the equatorial region to South Asian Coast during summer’ (Kundu and Mondal, 2019). The study of the simulation of the drought of Purulia is devoted to the micro level variability, which fluctuates seasonally. Therefore no prominent role of

ENSO and other phenomena have been assessed to illustrate the simulation of drought event in Purulia. Rather this research strongly encourages the local level factors viz. occurrence of tropical disturbances (Dhar *et al.*, 1981), several topographic variables such as local geology, relief, slope, soil and aspect (Basist *et al.*, 1994), increasing concentration of aerosol at lower atmosphere, changes in agricultural land use by means of initiation of irrigated agriculture (Douglas *et al.*, 2006) and deforestation (Nair *et al.*, 2003). Originally belonging to a granitic terrain, Purulia has crystalline basement rocks that are thinly covered by a weathered mantle (Baidya, 2015). The scattered shallow fracture zones of Purulia cannot store a sufficient quantity of groundwater (Dolui *et al.*, 2021). According to Mukherjee and Singh (2018), the groundwater of Purulia is restricted due to the weathered fracture zone. The fracture zone is having secondary porosity indicating a thick profile of in situ soft porous material developed as a disintegration product on the uppermost part of the

hard, consolidated rock due to weathering. Weathering generally imparts secondary porosity to the hard rock, which is fractured at the peninsular Purulia. According to Nag and Kundu (2016) relatively low groundwater level forms the depository of ground water as shallow aquifers in the area occupied by the hard rocks in Purulia.

## Conclusion

A comparison between Additive and Multiplicative Holt-Winter statistical method was carried out during 1979-2014 for Purulia and accuracy of each model was tested. In general, the trend of forecasted rainfall and SPI for both analysed models, was similar to the actual and forecasted models considering all the stations. Additive model was the most accurate model with relatively higher accuracy than the multiplicative model in simulating SPI over Purulia. Spatial assessment using both the models indicated the fact that in every post monsoon, monsoon and pre-monsoon phase, eastern and north eastern portions were more sensitive to drought whereas the western portions were at moderate to normal condition.

The comparative study of drought in seasonal aspect made the research interesting and unique. The identification and monitoring of the drought at seasonal aspect made the study a fruitful one for implementation. The study might also be very useful to improve the resiliency of the water management infrastructure, including a more accurate drought simulation tool for sustainable planning and assessment of drought of Purulia District.

## Conflict of interest

The authors declare that they have no conflict of interest.

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